## MA4529: MATHEMATICAL FINANCE

## Effective Term

Semester A 2022/23

## Part I Course Overview

Course Title
Mathematical Finance

## Subject Code

MA - Mathematics
Course Number
4529
Academic Unit
Mathematics (MA)
College/School
College of Science (SI)
Course Duration
One Semester
Credit Units
3
Level
B1, B2, B3, B4 - Bachelor's Degree
Medium of Instruction
English
Medium of Assessment
English
Prerequisites
MA3521 Introductory Mathematical Finance
Precursors
Nil
Equivalent Courses
Nil
Exclusive Courses
Nil

## Part II Course Details

## Abstract

This course provides fundamental concepts of probability theory, stochastic processes and option pricing. It helps students understand the mathematical concepts of stochastic processes and apply the knowledge to a range of problems in finance.

Course Intended Learning Outcomes (CILOs)

|  | CILOs | Weighting (if DEC-A1 app.) |  | DEC-A2 | DEC-A3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | explain clearly concepts from advanced probability and stochastic processes. | 15 | X |  |  |
| 2 | formulate financial phenomena in terms of Brownian motions and stochastic processes. | 15 | X | X |  |
| 3 | describe basic principles of quantitative finance, including no arbitrage and risk hedging. | 20 |  | X | X |
| 4 | apply the Black-Scholes formula in pricing options. | 15 |  | X |  |
| 5 | apply mathematical methods in deriving analytic relations among financial variables. | 15 |  | X | X |
| 6 | the combination of CILOs 1-5 | 20 | X | X | X |

## A1: Attitude

Develop an attitude of discovery/innovation/creativity, as demonstrated by students possessing a strong sense of curiosity, asking questions actively, challenging assumptions or engaging in inquiry together with teachers.

A2: Ability
Develop the ability/skill needed to discover/innovate/create, as demonstrated by students possessing critical thinking skills to assess ideas, acquiring research skills, synthesizing knowledge across disciplines or applying academic knowledge to real-life problems.

A3: Accomplishments
Demonstrate accomplishment of discovery/innovation/creativity through producing/constructing creative works/new artefacts, effective solutions to real-life problems or new processes.

Teaching and Learning Activities (TLAs)

| TLAs |  | Brief Description | CILO No. <br> applicable) |  |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Lectures | Learning through <br> teaching is primarily <br> based on lectures. | $1,2,3,4,5,6$ | 39 hours in total |
| 2 | Take-home assignments | Learning through take- <br> home assignments helps <br> students understand <br> advanced probability <br> theory, stochastic <br> processes, principles <br> of quantitative finance <br> and simple applications <br> in modeling financial <br> markets. | $1,2,3,4,5$ | after-class |

Assessment Tasks / Activities (ATs)

|  | ATs | CILO No. | Weighting (\%) | Remarks (e.g. Parameter for GenAI use) |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Test | 1, 2, 3 | 20 | Questions are designed for the first part of the course to see how well the students have learned concepts of advanced probability, stochastic processes and mathematical principles of financial economics. |
| 2 | Hand-in assignments | 1, 2, 3, 4, 5 | 10 | These are skills based assessment to help students understand advanced concepts of probability, stochastic processes and some applications in quantitative finance and option pricing. |
| 3 | Formative take-home assignments | 1, 2, 3, 4, 5 | 0 | The assignments provide students chances to demonstrate their achievements in applying concepts of mathematical finance learned from this course. |

## Continuous Assessment (\%)

30

## Examination (\%)

70

## Examination Duration (Hours)

3

## Additional Information for ATs

## 30\% Coursework

70\% Examination (Duration: 3 hours, at the end of the semester)
For a student to pass the course, at least $30 \%$ of the maximum mark for the examination must be obtained.

## Assessment Rubrics (AR)

## Assessment Task

1. Test

## Criterion

Ability in problem solving
Excellent (A+, A, A-)
High

Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate
Marginal (D)
Basic
Failure (F)
Not even reaching marginal levels

## Assessment Task

2. Hand-in assignments

Criterion
Understanding of concepts and applications
Excellent (A+, A, A-)
High
Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate
Marginal (D)
Basic
Failure (F)
Not even reaching marginal levels

## Assessment Task

3. Formative take-home assignments

## Criterion

Study attitude
Excellent (A+, A, A-)
High
Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate
Marginal (D)
Basic

## Failure (F)

Not even reaching marginal levels

## Assessment Task

4. Examination

## Criterion

Comprehensive ability in independent problem solving
Excellent (A+, A, A-)
High
Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate
Marginal (D)
Basic
Failure (F)
Not even reaching marginal levels

## Part III Other Information

## Keyword Syllabus

Contracts, Vanilla options, American type options, exotic options, put-call parity, no arbitrage, game theory, replicating portfolio, risk-free portfolio, binomial trees, martingale methods, Black-Scholes formulas, Itô' s lemma, stochastic derivatives, hedging portfolio.

## Reading List

Compulsory Readings

| Title |  |
| :--- | :--- |
| 1 | John C. Hull, Options, Futures, and other Derivatives, Prentice Hall. |
| 2 | Paul Wilmott, Sam Howison, and Jeff Dewynne, The Mathematics of Financial Derivatives, Cambridge University <br> Press. |

## Additional Readings

| Title |  |
| :--- | :--- |
| 1 | Rüdiger U. Seydel, Tools for Computational Finance, Springer. |

