## MA3523: INTRODUCTION TO ABSTRACT ALGEBRA

## Effective Term

Semester A 2022/23

## Part I Course Overview

Course Title
Introduction to Abstract Algebra

## Subject Code

MA - Mathematics
Course Number
3523
Academic Unit
Mathematics (MA)
College/School
College of Science (SI)
Course Duration
One Semester
Credit Units
3

Level
B1, B2, B3, B4 - Bachelor's Degree
Medium of Instruction
English
Medium of Assessment
English
Prerequisites
MA2503 Linear Algebra
Precursors
Nil
Equivalent Courses
Nil

Exclusive Courses
Nil

## Part II Course Details

## Abstract

The purpose of this course is to teach undergraduate student the fundamental concepts in abstract algebra, which are matrix operations, groups, vector spaces and linear transformations. The connection between matrix and group will be illustrated and practiced.

Course Intended Learning Outcomes (CILOs)

| CILOs |  | Weighting (if DEC-A1 <br> app.) |  | DEC-A2 |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | DEC-A3 |  |  |  |  |
| 1 | Fluent in matrix operations. | 10 | x | x |  |
| 2 | Explain the concept of group, subgroup and <br> homomorphism between groups. | 30 | x | x | x |
| 3 | Explain vector spaces in abstract field. | 15 | x | x |  |
| 4 | Solve linear transformations in terms of matrix <br> operations. | 15 | x | x |  |
| 5 | Explain deeper theories of group, for example, <br> the Sylow Theorem, generators and relations, <br> and apply to matrix operations. | 30 | x | x | x |

A1: Attitude
Develop an attitude of discovery/innovation/creativity, as demonstrated by students possessing a strong sense of curiosity, asking questions actively, challenging assumptions or engaging in inquiry together with teachers.

## A2: Ability

Develop the ability/skill needed to discover/innovate/create, as demonstrated by students possessing critical thinking skills to assess ideas, acquiring research skills, synthesizing knowledge across disciplines or applying academic knowledge to real-life problems.

A3: Accomplishments
Demonstrate accomplishment of discovery/innovation/creativity through producing/constructing creative works/new artefacts, effective solutions to real-life problems or new processes.

Teaching and Learning Activities (TLAs)

| TLAs |  | Brief Description |  | CILO No. <br> Hours/week (if <br> applicable) |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Lecture | Learning through <br> teaching is primarily <br> based on lectures | $1,2,3,4,5$ | 39 hours in total |
| 2 | Take-home assignments | Learning through take- <br> home assignments helps <br> students understand basic <br> concepts and theories of <br> group, vector space with <br> abstract field, and linear <br> transformations. | $1,2,3,4,5$ | after-class |

Assessment Tasks / Activities (ATs)

| ATs |  | CILO No. | Weighting (\%) <br> Remarks (e.g. Parameter <br> for GenAI use) |  |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Test (Mid Term Exam) | $1,2,3$ | 30 | Questions are designed <br> for the first part of the <br> course to see how well <br> students have learned the <br> concepts and theories of <br> matrix operations and <br> group. |
| 2 | Formative take-home <br> assignments | $1,2,3,4,5$ | 20 | The assignments provide <br> students chances to <br> demonstrate their <br> achievements on abstract <br> algebra learned in this <br> course. |

## Continuous Assessment (\%)

50
Examination (\%)
50

## Examination Duration (Hours)

2

## Additional Information for ATs

50\% Continuous Assessment(s)
$50 \%$ Examination (Duration: 2 hours, at the end of the semester)

For a student to pass the course, at least $30 \%$ of the maximum mark for the examination must be obtained.

## Assessment Rubrics (AR)

## Assessment Task

1. Test

## Criterion

ABILITY to APPLY and EXPLAIN the basic concepts and methodology of abstract algebra
Excellent (A+, A, A-)
High
Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate
Marginal (D)
Basic

## Failure (F)

Not even reaching marginal levels

## Assessment Task

2. Examination

## Criterion

ABILITY to DERIVE mathematical proofs in abstract algebra
Excellent (A+, A, A-)
High
Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate

Marginal (D)
Basic
Failure (F)
Not even reaching marginal levels

## Assessment Task

3. Formative take-home assignments

## Criterion

CAPACITY for LEARNING to understand the principles of abstract algebra
Excellent (A+, A, A-)
High
Good (B+, B, B-)
Significant
Fair (C+, C, C-)
Moderate
Marginal (D)
Basic
Failure (F)
Not even reaching marginal levels

## Part III Other Information

## Keyword Syllabus

Permutation matrix, group, subgroup, homorphism, quotient group, abstract field, the characteristic polynomial, rotation, operations on subsets, the Sylow Theorem, generators and relations.

## Reading List

Compulsory Readings
Title
1 "Algebra" by Michael Artin, Pearson (2rd edition), 2010.
Additional Readings

| Title |  |
| :--- | :--- |
| 1 | Nil |

