## MA3521: INTRODUCTORY MATHEMATICAL FINANCE

## Effective Term

Semester A 2023/24

## Part I Course Overview

Course Title
Introductory Mathematical Finance

## Subject Code

MA - Mathematics
Course Number
3521
Academic Unit
Mathematics (MA)
College/School
College of Science (SI)
Course Duration
One Semester
Credit Units
3
Level
B1, B2, B3, B4 - Bachelor's Degree
Medium of Instruction
English
Medium of Assessment
English

## Prerequisites

MA2506 Probability and Statistics; or MA2510 Probability and Statistics

Precursors
Nil

Equivalent Courses
Nil

Exclusive Courses

## Part II Course Details

## Abstract

This course introduces students to the financial instruments used in modern financial practice, particularly forward contracts and options. The emphasis is on developing the concept of risk-neutrality and the financial and mathematical theory underlying the behaviour of these financial instruments and preparing students with knowledge to solve related problems. Students should have a basic understanding of probability concepts to be properly prepared for this course.

Course Intended Learning Outcomes (CILOs)

|  | CILOs | Weighting (if DEC-A1 app.) |  | DEC-A2 | DEC-A3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | explain the concept of a forward contract, a call option and a put option, and recognize the mathematical and logical relationships among them. |  | x |  |  |
| 2 | apply the concept of no-arbitrage to the pricing of forward contracts. |  | x | x |  |
| 3 | describe the various basic option strategies (basic instrument of portfolio for trading strategies) and their objectives. |  | x | X | X |
| 4 | explain the concept of risk-neutrality and riskfree rate of interest. |  | x | X |  |
| 5 | construct a binomial tree for stock prices and apply it to evaluate the no-arbitrage price of an option and the assumptions needed for the price to be valid. |  | X | X | X |

## A1: Attitude

Develop an attitude of discovery/innovation/creativity, as demonstrated by students possessing a strong sense of curiosity, asking questions actively, challenging assumptions or engaging in inquiry together with teachers.

A2: Ability
Develop the ability/skill needed to discover/innovate/create, as demonstrated by students possessing critical thinking skills to assess ideas, acquiring research skills, synthesizing knowledge across disciplines or applying academic knowledge to real-life problems.

A3: Accomplishments
Demonstrate accomplishment of discovery/innovation/creativity through producing/constructing creative works/new artefacts, effective solutions to real-life problems or new processes.

## Teaching and Learning Activities (TLAs)

| TLAs |  | Brief Description | CILO No. | Hours/week (if <br> applicable) |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Lecture | Learning through <br> teaching is primarily <br> based on lectures. | $1,2,3,4,5$ | 39 hours in total |


| 2 | Take-home assignments | Learning through take- <br> home assignments helps <br> students implement <br> fundamental concepts <br> and theory of financial <br> instruments as well as <br> model their applications <br> in financial markets. | $1,2,3,4,5$ | after-class |
| :--- | :--- | :--- | :--- | :--- |
| 3 | Math Help Centre | Learning through project <br> helps students apply <br> principles of quantitative <br> finance and financial <br> economics to analyze <br> financial instruments in <br> contemporary financial <br> markets. It also helps <br> students to communicate <br> and collaborate effectively <br> in the team. | $1,2,3,4,5$ | after-class |

## Assessment Tasks / Activities (ATs)

| ATs |  | CILO No. | Weighting (\%) <br> Remarks (e.g. Parameter <br> for GenAI use) |  |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Test | $1,2,3$ | 20 | Questions are designed <br> for the first part of the <br> course to see how well <br> the students have learned <br> mathematical concepts <br> of forward contracts <br> and options, as well as <br> techniques of derivatives <br> pricing. |
| 2 | Hand-in assignments | $1,2,3,4,5$ | 10 | These are skills-based <br> assessment to help <br> students implement basic <br> concepts of quantitative <br> finance, mathematical <br> theory and pricing <br> strategies of financial <br> instruments. |

## Continuous Assessment (\%)

30

## Examination (\%)

70

## Examination Duration (Hours)

3

## Additional Information for ATs

30\% Coursework
70\% Examination (Duration: 3 hours, at the end of the semester)

For a student to pass the course, at least $30 \%$ of the maximum mark for the examination must be obtained.

## Assessment Rubrics (AR)

## Assessment Task

1. Test

Criterion
ABILITY to APPLY the fundamental concepts and methodology of financial derivatives, option pricing and risk hedging
Excellent (A+, A, A-)
High
Demonstrate an excellent understanding of Pricing model and can always apply this understanding to different financial derivatives.

## Good (B+, B, B-)

Significant
Demonstrate an understanding of Pricing model and can usually apply this understanding to different financial derivatives.

Fair (C+, C, C-)
Moderate
Demonstrate a partial understanding of Pricing model and can sometimes apply this understanding to different financial derivatives.

## Marginal (D)

Basic
Demonstrate little understanding of Pricing model and can rarely apply this understanding to different financial derivatives.

Failure (F)
Not even reaching marginal levels

## Assessment Task

2. Hand-in assignments

## Criterion

CAPACITY for LEARNING to understand and apply the principles and different methods of mathematic finance

## Excellent (A+, A, A-)

High
Well organized with correct answers.
Good (B+, B, B-)
Significant
Organized and most answers are correct.
Fair (C+, C, C-)
Moderate
Organization needs to improve, some correct answers.

## Marginal (D)

Basic
Very weak evidence of organization, a few correct answers.

## Failure (F)

Not even reaching marginal levels

## Assessment Task

4. Examination

## Criterion

ABILITY to APPLY the fundamental concepts and methodology for the comprehensive problem solving of mathematic finance

## Excellent (A+, A, A-)

High
Well organized. with correct answers. Mathematical terms and symbols are often elaborated upon.

## Good (B+, B, B-)

Significant
Organized and most answers are correct. Mathematical terms and symbols are used appropriately.
Fair (C+, C, C-)
Moderate
Organization needs to improve, some correct answers. Some mathematical terms and symbols are used correctly.

## Marginal (D)

Basic
Very weak evidence of organization, a few correct answers.
Mathematical terms and symbols are weak, not even refers to mathematical terms are used.

## Failure (F)

Not even reaching marginal levels

## Part III Other Information

## Keyword Syllabus

- Forward contracts, options, payoff, and no-arbitrage profit;
- Option strategies and combinations;
- Interest rate and Risk-neutrality;
- Call and Put options, put-call parity on options;
- Binomial tree for stock option pricing model: Random Walk, Brownian Motion, Martingale;
- Binomial tree for pricing exotic options such as barrier option and Asian option.


## Reading List

Compulsory Readings

| Title |  |
| :--- | :--- |
| 1 | John C. Hull, Options, Futures, and other Derivatives, Prentice Hall. |

Additional Readings

| Title |  |
| :--- | :--- |
| 1 | Robert L. McDonald, Derivatives Markets. Addison-Wesley. |

