City University of Hong Kong Course Syllabus

offered by School of Data Science with effect from Semester A 2021 / 22

| Part I Course Over | view |
|---|---------------------|
| Course Title: | Advanced Statistics |
| Course Code: | SDSC8004 |
| Course Duration: | One semester |
| Credit Units: | 3 |
| Level: | R8 |
| Medium of Instruction: | English |
| Medium of Assessment: | English |
| Prerequisites: (Course Code and Title) | Nil |
| Precursors: (Course Code and Title) | Nil |
| Equivalent Courses: (Course Code and Title) | Nil |
| Exclusive Courses: (Course Code and Title) | Nil |

Part II Course Details

1. Abstract

This course aims to provide students with a solid foundation of statistical concepts, theory, and methods including probability theory, statistical estimation and inference methods, and multivariate statistics. It also aims to provide students with a rigorous introduction to the theory and implementation of statistical models such as linear models, generalized linear models, and nonparametric models. Emphasis will be placed on rigorous mathematical derivations, understanding of the fundamentals of statistics but implementation of the statistical methods via computer programming in R or Matlab will be an important part of the course as well.

2. Course Intended Learning Outcomes (CILOs)

| No. | CILOs# | Weighting | Discovery-enriched curriculum related learning outcomes | | |
|-----|---|-----------|---|----------|-----------|
| | | | A1 | A2 | <i>A3</i> |
| 1. | Prove and apply various fundamental results in probability theory. | 20% | ✓ | √ | |
| 2. | Understand and implement the techniques of parametric inference such as maximum likelihood estimation and Bayesian inference. | 25% | √ | ✓ | |
| 3. | Understand and derive key results in the theory of linear models and linear model selection. | 25% | ✓ | ✓ | |
| 4. | Understand and derive key results in the theory of nonparametric statistical models and methods such as the bootstrap method and Gaussian process regression. | 20% | √ | ✓ | |
| 5. | Implement statistical inference methods and modelling methodologies with computer codes. | 10% | √ | √ | |
| | | 100% | | | |

A1: Attitude

Develop an attitude of discovery/innovation/creativity, as demonstrated by students possessing a strong sense of curiosity, asking questions actively, challenging assumptions or engaging in inquiry together with teachers.

A2: Ability

Develop the ability/skill needed to discover/innovate/create, as demonstrated by students possessing critical thinking skills to assess ideas, acquiring research skills, synthesizing knowledge across disciplines or applying academic knowledge to self-life problems.

A3: Accomplishments

Demonstrate accomplishment of discovery/innovation/creativity through producing /constructing creative works/new artefacts, effective solutions to real-life problems or new processes.

3. Teaching and Learning Activities (TLAs)

| TLA | Brief Description | CIL | CILO No. | | Hours/week | | |
|---------------------------|---|----------|----------|----------|------------|----------|-------------------|
| | | 1 | 2 | 3 | 4 | 5 | |
| Large Class Activities | Lectures, software training, and in-class exercises | ✓ | √ | ✓ | ✓ | ✓ | 26 hours/semester |
| Assignments | Exercises provide students with the opportunities to familiarize and apply the statistical tools learnt during the lectures | ✓ | ✓ | ✓ | ✓ | ✓ | 12 hours/semester |

4. Assessment Tasks/Activities (ATs)

| Assessment Tasks/Activities | CILO No. | | | | | Weighting | Remarks |
|---|----------|----------|----------|----------|----------|-----------|---------|
| | 1 | 2 | 3 | 4 | 5 | | |
| Continuous Assessment: <u>75</u> % | | | | | | | |
| <u>Midterm</u> | | | | | | 25% | |
| Students will be assessed via the midterm | | | | | | | |
| their understanding of concepts, theory, | ✓ | ✓ | ✓ | ✓ | | | |
| and methods learned in class, textbooks, | | | | | | | |
| reading materials and their ability to apply | | | | | | | |
| subject-related knowledge. | | | | | | 500/ | |
| Two assignments Students will work individually to derive | | | | | | 50% | |
| or prove results in probability and | | | | | | | |
| statistical theory, and apply statistical | ✓ | ✓ | ✓ | √ | ✓ | | |
| methods to analyse data with the help of | | | | | | | |
| software. | | | | | | | |
| Examination: 25 % (duration: 3 Hours) | | | | | | 1 | |
| Examination | | | | | | 25% | |
| Students will be assessed via the | | | | | | | |
| examination their understanding of | | | | | | | |
| concepts, theory, and methods learned in | ✓ | ✓ | ✓ | √ | | | |
| class, textbooks, reading materials and | | | | | | | |
| their ability to apply subject-related | | | | | | | |
| knowledge. | | | | | | | |
| | | | | | | | |

100%

5. Assessment Rubrics

| Assessment Task | Criterion | Excellent | Good | Fair | Marginal | Failure |
|-----------------|--|-------------|-------------|-------------|----------|-----------------------------------|
| | | (A+, A, A-) | (B+, B, B-) | (C+, C, C-) | (D) | (F) |
| 1. Coursework | Midterm and assignments | High | Significant | Moderate | Basic | Not even reaching marginal levels |
| 2. Examination | Examination questions are designed to assess student's level of achievement of the intended learning outcomes. Students will need to demonstrate understanding of various elements of statistical theory and methods taught in the course through precise mathematical exposition. | High | Significant | Moderate | Basic | Not even reaching marginal levels |

Part III Other Information (more details can be provided separately in the teaching plan)

1. Keyword Syllabus

- Probability theory and distributions (probability space, random variables, expectation, inequalities, and convergence of random variables)
- Parametric statistical inference theory and methods (maximum likelihood estimation, Fisher's scoring, Fisher information, consistency and limiting distribution of maximum likelihood estimators, statistical decision theory, Rao-Blackwell theorem, minimum variance unbiased estimation, Bayesian inference)
- Multivariate statistics (covariance matrix estimation, James-Stein estimator, principle components analysis), linear model theory (least squares, Gauss Markov theorem, ridge regression, leave-one-out cross validation, optimal design of experiments), variable selection methods (Bayesian information criterion, LASSO, LARS).
- Nonparametric statistical models and methods (bootstrap, Gaussian process models, local polynomial regression, kernel methods)

2. Reading List

2.1 Compulsory Readings

| 1. | Wasserman, L. (2013). All of statistics: a concise course in statistical inference. Springer |
|----|--|
| | Science & Business Media. |
| 2. | Keener, R. W. (2011). Theoretical statistics: Topics for a core course. Springer. |
| 3. | Resnick, S. I. (2013). A probability path. Springer Science & Business Media. |
| 4. | Casella, G., & Berger, R. L. (2002). Statistical inference (Vol. 2). Pacific Grove, CA: |
| | Duxbury. |
| 5. | Rasmussen, C. E., & Williams, C. K. (2006). Gaussian Process Regression for Machine |
| | Learning. The MIT Press |

2.2 Additional Readings

NIL