

Department of Mathematics

# **DEPARTMENT OF MATHEMATICS** City University of Hong Kong

## Inverse problems for non-linear partial differential equations

by

### **Professor Matti LASSAS** University of Helsinki

### Date: 24 Feb. 2022 (Thursday) Time: 4:00 – 5:00 pm

#### ABSTRACT

In the talk we give an overview on how inverse problems can be used solved using non-linear interaction of the solutions. This method can be used for several different inverse problems for nonlinear hyperbolic or elliptic equations. In this approach one does not consider the non-linearity as a troublesome perturbation term, but as an effect that aids in solving the problem. Using it, one can solve inverse problems for non-linear equations for which the corresponding problem for linear equations is still unsolved. For the hyperbolic equations, we consider the non-linear wave equation \$\square g u+u^m=f\$ on a Lorentzian manifold \$M\times R\$ and the source-to-solution map \$\Lambda\_V:f\to u|\_V\$ that maps a source \$f\$, supported in an open domain \$V\subset M\times R\$, to the restriction of \$u\$ in \$V\$. Under suitable conditions, we show that the observations in \$V\$, that is, the map \$\Lambda V\$, determine the metric \$g\$ in a larger domain which is the maximal domain where signals sent from \$V\$ can propagate and return back to \$V\$. We apply non-linear interaction of solutions of the linearized equation also to study non-linear elliptic equations. For example, we consider \$\Delta g u+qu^m=0\$ in \$\Omega\subset R^n\$ with the boundary condition \$u| {\partial \Omega}=f\$. For this equation we define the Dirichlet-to-Neumann map \$\Lambda {\partial \Omega}:f\to u|\_V\$. Using the high-order interaction of the solutions, we consider various inverse problems for the metric \$g\$ and the potential \$q\$.

**Registration URL:** 

https://cityu.zoom.us/meeting/register/tJApc-GqqzkuGd3Lhyw1W6bkd470yNF4t3xY

