

# Anti-resonant fiber with high-resistivity silicon for THz wave transmission

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**A novel anti-resonant fiber for low-loss terahertz waveguides is proposed and analyzed. The terahertz fiber uses high-resistivity silicon as the bulk material and nine nested double-layer concentric circular tubes in the cladding to reduce propagation losses. The effects of the geometric parameters on the propagation characteristics are analyzed by the finite element method. The result indicates that an ultra-low total loss of  $4.9 \times 10^{-4}$  dB/m is achieved at  $f = 1$  THz. The low-loss propagation window is 0.48 THz ranging from 0.6 to 1.4 THz. In addition, the influence of mechanical bending on the propagation loss is investigated and the bending loss can be maintained at less than  $7.3 \times 10^{-3}$  dB/m at  $f = 1$  THz even if the bending radius is larger than 60 cm. The properties of this anti-resonant fiber are significantly superior to those of previously reported structures and the fiber thus has large commercial potential.** © 2023 Optica Publishing Group

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## 1. INTRODUCTION

As a kind of special fiber, hollow-core fibers (HCFs) have the advantages of low nonlinearity, low dispersion, low material absorption loss, high damage thresholds, and low propagation latency [1] as well as some applications in high power delivery [2], high-speed data communication [3], ultra-short pulse delivery [4], pulse compression [5], supercontinuum [6], gas fiber lasers [7], and gas nonlinear optics [8]. HCFs mainly include photonic bandgap fibers [9] (PBGFs) and anti-resonant fibers [10] (ARFs). The PBGFs utilize periodically arranged air holes in the cladding to confine the light in the core, and the propagation loss can be reduced by adjusting the cladding structure. However, the propagation windows of PBGFs are usually relatively limited, whereas ARFs can overcome the window limitation and exhibit favorable propagation properties, including small nonlinearity, low propagation loss, and controllable dispersion [11].

The ARFs are on the basis of the “Fano resonance” mechanism which prevents the coupling between the core mode and cladding modes to realize light propagation in various spectral bands. Owing to the particularity of the terahertz (THz) regime, the propagation losses of reported THz ARFs are relatively high. Setti *et al.* fabricated a THz ARF consisting of six single-layer circular tubes constructed with PMMA [12] and observed a total loss of 16 dB/m at  $f = 0.828$  THz.

Hasanuzzaman *et al.* designed a THz ARF composed of six nested circular tubes based on Topas [13]. The confinement loss (CL) is only  $3.4307 \times 10^{-4}$  dB/m, but the total loss reaches 0.05 dB/m at  $f = 1$  THz due to the larger effective material loss. The low-loss propagation window is 0.4 THz. Mollah *et al.* simulated a THz ARF with six half circular tubes and half elliptical tubes using Zeonex [14]. The confinement loss of the order of  $10^{-4}$  dB/m and the effective material loss (EML) of 0.034 dB/m can be achieved at  $f = 1$  THz. The total loss of the fiber is 0.034 dB/m, which is mainly determined by the effective material loss, and the low-loss propagation window is 0.5 THz. Sultana *et al.* numerically analyzed three THz ARFs composed of nonnested circular tubes, nested circular tubes, and adjacent nested circular tubes based on Zeonex [15]. The results show that the THz ARF with five nested circular tubes has a relatively low total loss of 0.055 dB/m at  $f = 1$  THz. Comparison of these results reveals that the effective material losses of these above-mentioned THz ARFs are still not mitigated inadequately. Therefore, we proposed a THz ARF using six nested double-layer U-shape tubes in conjunction with high-resistivity silicon (HRS) [16]. The refractive index is considered as a constant of 3.417 in the 0.5–4.5 THz range and the bulk material absorption loss is less than  $1.5 \text{ m}^{-1}$  in the range of 0.1–1.5 THz [17], which is much less than that of  $27.6 \text{ m}^{-1}$  and  $20 \text{ m}^{-1}$  for Topas [13] and Zeonex [14] around 1 THz.

The HRS has been used in designing photonic crystal fibers in the terahertz regime [18–20]. The optimized fiber shows an effective material loss of  $5 \times 10^{-4}$  dB/m and a confinement loss of  $2.6 \times 10^{-3}$  dB/m, achieving a total loss of  $3.1 \times 10^{-3}$  dB/m at  $f = 1$  THz and a low-loss propagation window of 0.44 THz. However, it is difficult to further reduce the confinement loss due to the ultra-high refractive index of HRS.

Herein, a THz ARF based on HRS with nine nested double-layer concentric circular tubes is designed and analyzed. This structure reduces the confinement loss to  $2.6 \times 10^{-4}$  dB/m. The effective material loss is only  $2.3 \times 10^{-4}$  dB/m and the total loss reaches  $10^{-4}$  dB/m for the first time in the frequency ranges of 0.88–0.92 THz and 0.96–1.14 THz. Moreover, the ARF exhibits good bending resistance, as manifested by a bending loss of less than  $7.3 \times 10^{-3}$  dB/m at  $f = 1$  THz in spite of the bending radius being larger than 60 cm.

### 2. GEOMETRY OF THE PROPOSED FIBER

The cross section of the proposed ARF structure is illustrated in Fig. 1. The core diameter is  $D_c = 6.2$  mm, and the external and internal layer diameters are  $d_1 = 2.4$  mm and  $d_2 = 1.5$  mm, respectively. A large core diameter will result in a high bending loss due to the large mode field area. Therefore, our proposed fiber uses a nine-tube structure to suppress bending loss caused by the large core diameter. The cladding consists of nine nested double-layer concentric circular tubes connected by solid supporting rods. This structure can better maintain the concentricity and stability of the ARF, avoiding fiber deformation. The uniform anti-resonant wall thickness of the cladding structure is  $t = 0.035$  mm. The thicknesses of the jacket tube and perfectly matched layer are  $JT = 0.15$  mm and  $T = 0.5$  mm, respectively, and the internal radius of the ARF is  $R_i = 5.5$  mm. In order to ensure accurate numerical calculations, extremely fine mesh sizes of  $\lambda/6$  and  $\lambda/4$  are adopted in the HRS and air parts, respectively [21,22].

### 3. ANALYSIS AND DISCUSSION

According to the principle of the anti-resonant reflecting optical waveguide, light propagation in the core will generate higher losses at the resonant frequencies and hence, it is essential to

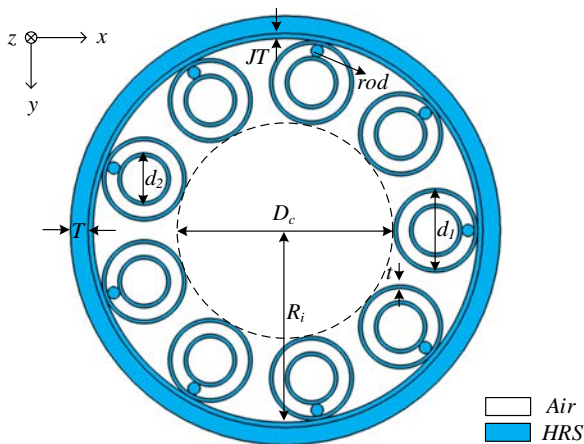


Fig. 1. Cross section of the ARF.

avoid the resonant frequency to obtain a lower propagation loss and wider propagation window, which can be calculated by Eq. (1) [23–26]:

$$f_c = \frac{mc}{2t\sqrt{n^2 - 1}}, \quad (1)$$

where  $c$  represents the velocity of light in vacuum,  $m$  represents the order of resonance,  $n$  represents the refractive index of the bulk material, and  $t$  represents the wall thickness.

The confinement loss (CL) and effective material loss (EML) of the THz ARF can be shown by Eqs. (2) and (3) [27–30]:

$$CL = 8.686 \left( \frac{2\pi f}{c} \right) \text{Im}(n_{\text{eff}}), \quad [\text{dB/m}], \quad (2)$$

$$\text{EML} = 4.34 \sqrt{\frac{\varepsilon_0}{\mu_0}} \frac{\int_{A_{\text{mat}}} n \alpha_{\text{mat}} |E|^2 dA}{2 \int_{A_{\text{all}}} S_z dA}, \quad [\text{dB/m}], \quad (3)$$

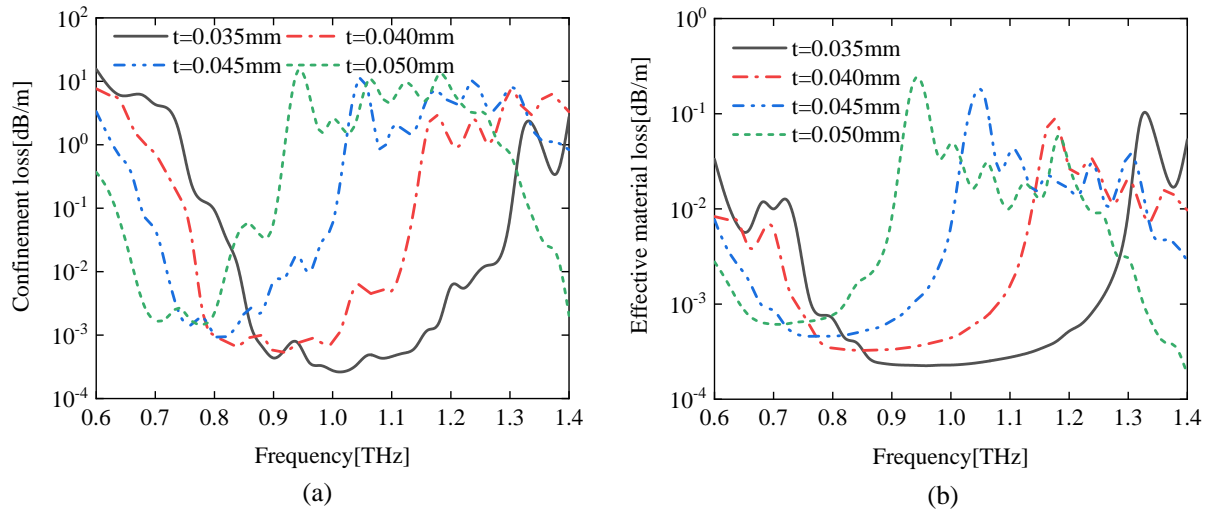
where  $f$  is the operating frequency;  $\text{Im}(n_{\text{eff}})$  is the imaginary part of the effective refractive index;  $\varepsilon_0$  and  $\mu_0$  are the permittivity and permeability in vacuum, respectively;  $\alpha_{\text{mat}}$  is the bulk material absorption loss; and  $S_z$  is the Poynting vector along the propagation direction of  $z$ , which is defined as  $S_z = \frac{1}{2} \text{Re}(E \times H^*)z$ , where  $E$  is the electric field and  $H$  is the magnetic field.

The influence of the wall thickness  $t$  of the nested concentric circular tubes on the propagation loss properties is analyzed. For  $R_i = 5.5$  mm,  $JT = 0.15$  mm,  $D_c = 6.2$  mm,  $d_1 = 2.4$  mm, and  $d_2 = 1.5$  mm, the spectra in Fig. 2(a) present the CL for various wall thicknesses. The low-loss band of the CL spectra ( $< 10^{-1}$  dB/m) is narrowest, and the smallest CL is  $1.4 \times 10^{-3}$  dB/m as  $t = 0.05$  mm. With decreasing the wall thickness, the CL spectra shift to higher frequency direction.

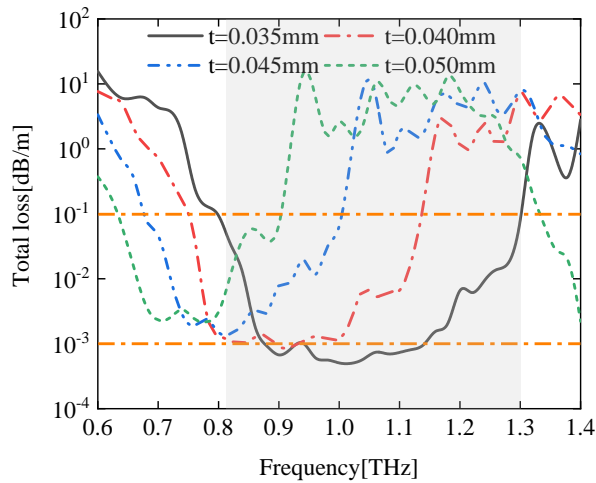
The CL decreases progressively, and the low-loss band broadens. The reason for this phenomenon is that a thinner wall produces a higher resonant frequency according to Eq. (1), and the low-loss band is broader. Meanwhile the nested double-layer tubes result in numerous oscillation peaks due to the intense couplings between the external and internal layer concentric circular tubes [31]. The low-loss band of the CL spectra is broadest, and the lowest CL is  $2.5 \times 10^{-4}$  dB/m as  $t = 0.035$  mm. The spectra in Fig. 2(b) exhibit EMLs for various wall thicknesses. As the wall thickness decreases, the EML spectra exhibit a similar trend as the CL spectra. The lowest EML is  $2.3 \times 10^{-4}$  dB/m.

The total loss (TL) spectra for various wall thicknesses can be obtained by superposing the CL and EML spectra, as shown in Fig. 3. With decreasing the wall thickness, the lowest TL decreases progressively. For  $t = 0.035$  mm, the lowest TL is only  $4.8 \times 10^{-4}$  dB/m. The low-loss window ( $< 10^{-1}$  dB/m) also increases as the wall thickness decreases. As  $t = 0.035$  mm, the low-loss propagation window is 0.48 THz, and the frequency being less than  $10^{-3}$  dB/m is 0.22 THz. Hence, our ARF reduces the propagation loss and achieves a wide window and low-loss propagation at the same time.

For  $R_i = 5.5$  mm,  $JT = 0.15$  mm,  $d_2 = 1.5$  mm, and  $t = 0.035$  mm, the impact of the external layer diameter  $d_1$  of the nested concentric circular tubes on the propagation loss properties is illustrated in Fig. 4(a). When  $d_1 = 2$  mm, the low-loss window of the ARF is narrowest. As the external

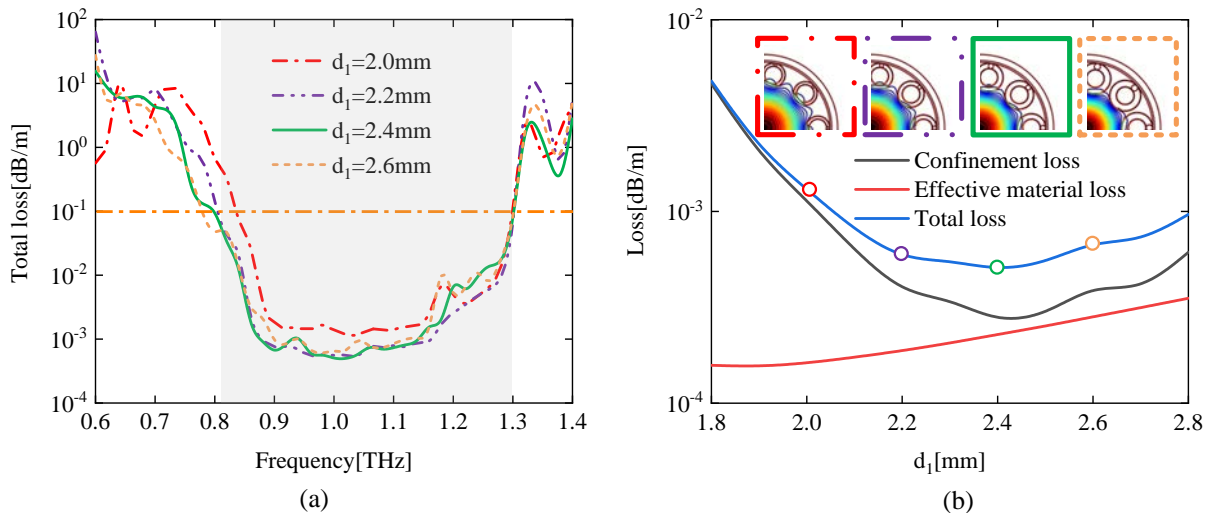


**Fig. 2.** (a) CL and (b) EML versus frequencies for various wall thicknesses.

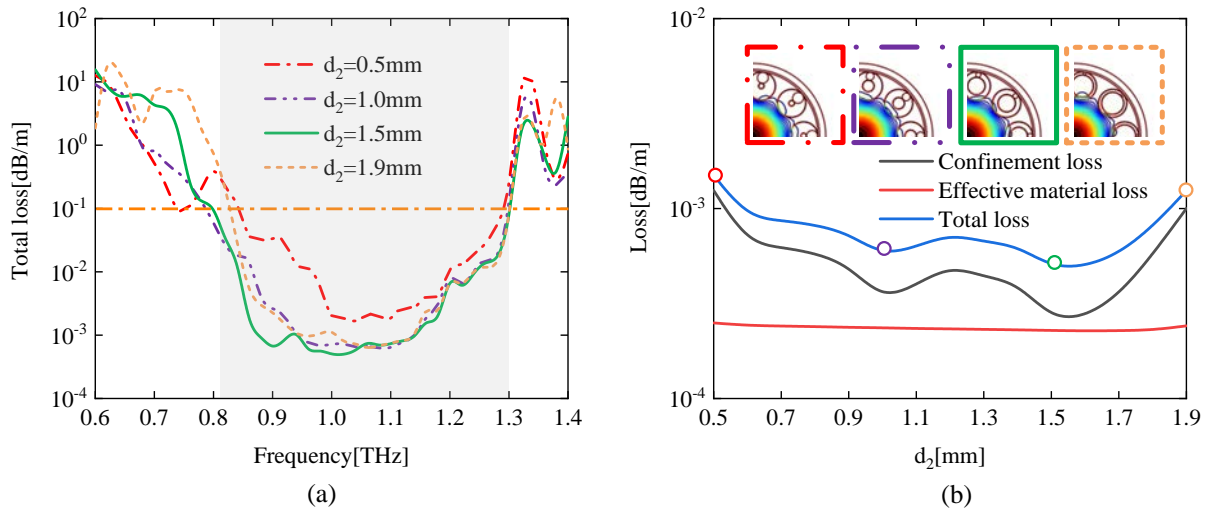


**Fig. 3.** TL versus frequencies for various wall thicknesses.

layer diameter goes up, the difference of the TL spectra for  $d_1 = 2.2$  mm, 2.4 mm, and 2.6 mm is smaller. In order to determine the optimal  $d_1$ , the CL, EML, and TL for various external layer diameters at  $f = 1$  THz are derived as manifested in Fig. 4(b). Compared to the CL, the EML exhibits a smaller effect as shown by the solid red curve. The solid blue curve presents the TL, and the insets show the contour plots of the mode fields for various external layer diameters. The TL decreases as the external layer diameter increases initially and then increases slowly. It is because when the external layer diameter is relatively small, the distance between adjacent tubes is large and it is easier for the mode field to leak through the gap to produce greater losses, as shown in the inset signed by the red border curve. As the external layer diameter goes up, the mode field is restricted in the core as presented in the contour plots of the mode field (purple and green border curves). As the external layer diameter continues to increase, the loss increases slightly due to additional resonance between adjacent tubes [32].



**Fig. 4.** (a) TL versus frequencies for various external layer diameters and (b) loss versus external layer diameters at  $f = 1$  THz.

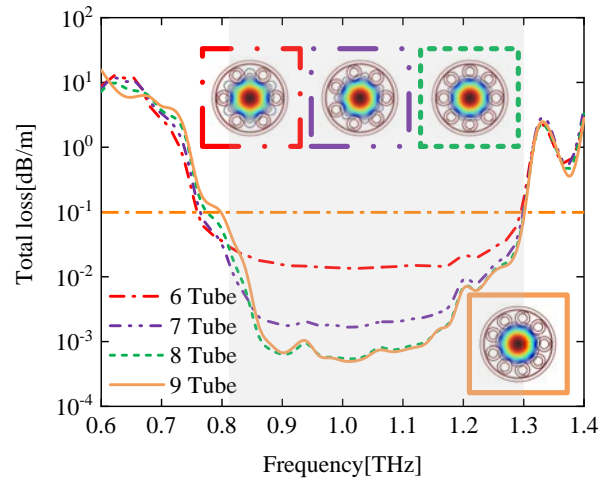


**Fig. 5.** (a) TL versus frequencies for various internal layer diameters and (b) loss versus internal layer diameters at  $f = 1$  THz.

Therefore,  $d_1 = 2.4$  mm shows the smallest TL and is selected to be the preferred value.

The impact of the internal layer diameter  $d_2$  of the nested concentric circular tubes on the propagation loss properties is derived and displayed in Fig. 5(a). When the internal layer diameter is relatively small ( $d_2 = 0.5$  mm), the lowest loss is slightly higher, and the value is  $1.4 \times 10^{-3}$  dB/m. As the internal layer diameter goes up, the TL spectra show smaller differences for  $d_2 = 1.0$  mm, 1.5 mm, and 1.9 mm. This is because the double-layer anti-resonant effect can better restrict the mode field in the core [33]. To determine the optimal  $d_2$ , the CL, EML, and TL for various internal layer diameters at  $f = 1$  THz are derived and displayed in Fig. 5(b). The internal layer diameter hardly influences the EML, but has a significant impact on the CL. The solid blue curve represents the TL, and the insets display the contour plots of the mode fields for various internal layer diameters. The mode field is limited in the core for  $d_2 = 1.5$  mm, which corresponds to the lowest TL and is selected to be the preferred value.

The effect of the quantity of the nested concentric circular tubes on the propagation loss properties is investigated. As for  $R_i = 5.5$  mm,  $JT = 0.15$  mm,  $D_c = 6.2$  mm,  $d_1 = 2.4$  mm,  $d_2 = 1.5$  mm, and  $t = 0.035$  mm, the TL spectra and the contour plots of the mode field for various quantities of tubes are shown in Fig. 6. As the quantity of the nested concentric circular tubes is six, the mode field is not limited in the core due to the larger distance between adjacent tubes revealed by the contour plots of the mode field (red frame) at  $f = 1$  THz. The smallest TL is  $1.3 \times 10^{-2}$  dB/m. As the amount of the nested concentric circular tubes is seven, the distance between adjacent tubes decreases resulting in smaller mode field leakage, as shown in the purple inset. The smallest value in the TL spectra is  $1.6 \times 10^{-3}$  dB/m. As the numbers of the nested concentric circular tubes are eight and nine, the TL spectra show almost the same trend. The insets marked by the green and orange frames are also consistent, indicating that the mode field is limited in the core. It means that more tubes can avoid mode field leakage through the gap of the adjacent tubes for large core ARF and the TL can be controlled.



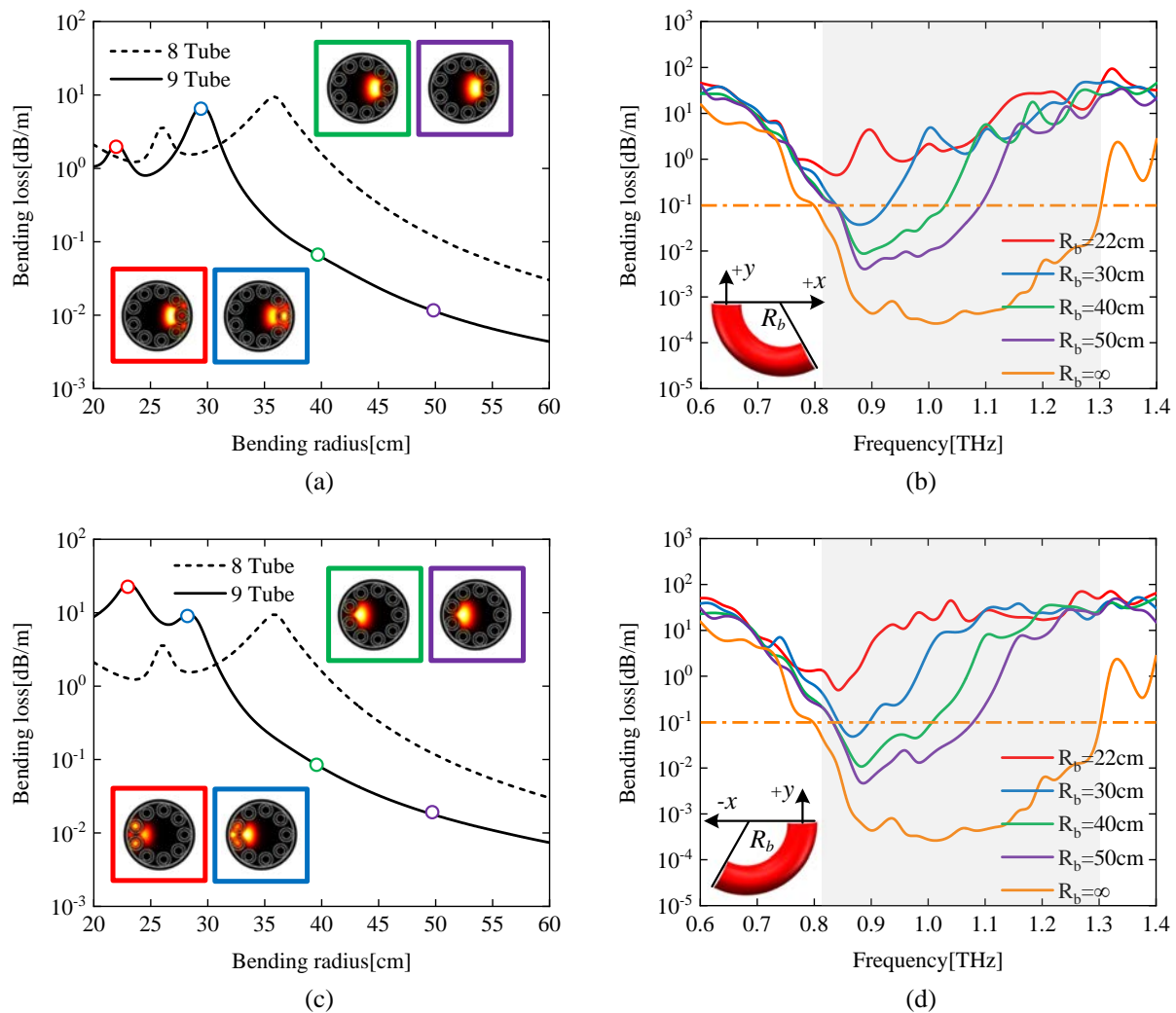
**Fig. 6.** TL versus frequencies for various quantities of tubes.

In order to further compare and optimize the eight-tube and nine-tube structures, the bending characteristic of the THz ARF is analyzed. By the conformal transformation method, we use an equivalent refractive index  $n_{eq}$  to compute bending loss expressed by Eq. (4) [34,35]:

$$n_{eq} = n \exp[x \cos \theta + y \sin \theta / R_b], \tag{4}$$

where  $n$  denotes the refractive index distribution of straight fiber cross section,  $R_b$  denotes the bending radius, and  $\theta$  denotes the bending angle referred to an angle between the bending axis and positive  $x$  axis. The bending loss can be calculated by taking the  $n_{eq}$  into Eq. (2).

As the bending angle  $\theta$  is  $0^\circ$  (along the  $x$  direction) and  $180^\circ$  (along the  $-x$  direction), the bending losses of the eight-tube and nine-tube structures for various bending radii at  $f = 1$  THz are depicted in Figs. 7(a) and 7(c). The bending loss of the nine-tube structure is lower demonstrating good bending resistance. Therefore, the nine-tube cladding is selected as the optimal structure and the bending characteristics are further analyzed. When the ARF is bent, the mode field in the core



**Fig. 7.** (a) Bending losses at a bending angle  $\theta = 0^\circ$  versus radii at  $f = 1$  THz, (b) bending losses at a bending angle  $\theta = 0^\circ$  versus frequencies for various bending radii, (c) bending losses at a bending angle  $\theta = 180^\circ$  versus radii at  $f = 1$  THz, and (d) bending losses at a bending angle  $\theta = 180^\circ$  versus frequencies for various bending radii.

deviates radially toward the bending direction. The mode field is still concentrated in the core for a larger bending radius presented in the green and purple insets of Figs. 7(a) and 7(c). However, the bending loss goes up progressively with going down bending radius and higher loss peaks occur. The red and blue insets show that the mode fields in the core partially leak to the cladding. The loss peaks due to resonances between the core mode and cladding modes appear when the phases of the modes match [12].

Figures 7(b) and 7(d) show the bending loss spectra for bending angles of  $\theta = 0^\circ$  and  $180^\circ$  for various bending radii. When  $R_b = 22$  cm, the bending loss spectrum has no low-loss band. The phenomenon mainly stems from the fact that bending disrupts the central symmetric structure of straight fiber and distorts the refractive index distribution to increase the bending loss [15]. When  $R_b = 30$  cm, the bending loss decreases, and the low-loss band appears. A larger bending radius leads to a wider low-loss band. When the bending radius approaches infinity, the low-loss window is the widest and the loss is the lowest. Table 1 compares the propagation characteristics between our ARF and

previously reported ARFs. It can be observed that our large core ARF reduces the EML and suppresses the CL giving rise to an ultra-low TL of  $10^{-4}$  dB/m. The performance is better than the previous small core ARF [16]. The proposed fiber shows improved propagation characteristic as a terahertz waveguide. The flexibility and bendability of this fiber can be improved by adding a coating layer.

#### 4. CONCLUSION

An ARF consisting of nine nested double-layer concentric circular tubes is presented and investigated. The HRS decreases the EML in the terahertz spectral range and the ARF structure suppresses the CL. The CL and EML are as low as  $2.6 \times 10^{-4}$  dB/m and  $2.3 \times 10^{-4}$  dB/m at  $f = 1$  THz, respectively. The TL reaches the order of  $10^{-4}$  dB/m for the first time, and the low-loss propagation window is 0.48 THz. At the same time, the ARF exhibits good bending resistance. As the bending radius is larger than 60 cm, the bending loss at

Table 1. Comparison between Our ARF and Previously Reported ARFs

Reference	Material Type	CL (dB/m)	EML (dB/m)	TL (dB/m)	Propagation Window (THz)	Operating Frequency (THz)
Ref. [36]	PMMA	8	/	/	/	2.52
Ref. [37]	HDPE	7	/	/	/	2.52
Ref. [12]	PMMA	/	/	16	/	0.828
Ref. [13]	Topas	$3.4307 \times 10^{-4}$	0.05	0.05	0.4	1.0
Ref. [38]	Topas	$3.2 \times 10^{-4}$	/	/	/	2.44
Ref. [14]	Zeonex	$\sim 10^{-4}$	0.034	0.034	0.5	1.0
Ref. [15]	Zeonex	/	0.055	0.055	/	1.0
Ref. [16]	HRS	$2.6 \times 10^{-3}$	$5 \times 10^{-4}$	$3.1 \times 10^{-3}$	0.44	1.0
This work	HRS	$2.6 \times 10^{-4}$	$2.3 \times 10^{-4}$	$4.9 \times 10^{-4}$	0.48	1.0

$f = 1$  THz is less than  $7.3 \times 10^{-3}$  dB/m. The excellent performance of the ARF suggests enormous application potential for terahertz waveguides.

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**Disclosures.** The authors declare no conflicts of interest.

**Data availability.** Data underlying the results presented in this paper are not publicly available at this time but may be obtained from the authors upon reasonable request.

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