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Abstract: Based on two parallel photonic crystal fibers (PCFs) with D-shape structure, a novel surface plasmon resonance (SPR) sensor with low refractive index (RI) detection at near-infrared wavelengths is described. According to the coupled-mode theory, directional power transfer between the two fiber cores is enhanced by resonant coupling between the surface plasmon modes and fiber core-guided modes. In comparison with corresponding single D-shape PCF, a maximum spectral sensitivity up to 13 500 nm/RIU and resolution of 7.41 \times 10^{-6} RIU for RI detection range between 1.27 and 1.32 are achieved. The proposed two parallel D-shape PCFs-SPR sensor with lower RI detection range offer large potential in the fields of pharmaceutical inspection and pharmaceutical leakage monitoring.

Index Terms: PCF-SPR, parallel fiber, near-infrared, lower RI detection.

1. Introduction
Surface plasmon resonance is an effective sensing technology and has been widely applied in biotechnology, medical diagnostics, and environmental monitoring owing to its extreme sensitivity to refractive index variations [1]–[3]. Based on optical fiber SPR sensors, the D-shape [4], cladding-off [5], single mode fiber (SMF) [6], Bragg grating fiber [7], and photonic crystal fiber (PCF) [8]–[10] have been demonstrated theoretically and experimentally. Among them, PCF based-SPR (PCF-SPR) sensors have a great deal of advantages over conventional optical fiber SPR sensors including small size, flexible structural design, high sensitivity, and phase-matching condition. To implement PCF-SPR sensors, the metal layers and the analyte usually must be filled inside the fiber but the analyte in the PCF holes is difficult to change. In order to enhance the penetration of metal coating and sensing media inside the fiber, the sensing method of an external coating PCF has been
put forward. Metal layers/sensing media have been placed outside the fiber, which simplifies the fabrication process and sensing mechanism [11].

Spurred by advances in micro-fabrication technology, the D-shape PCFs are experimentally available. The D-shape PCF-SPR have attracted much interest for their unique performances [12], [13]. N. Luan et al. [14] proposed the D-shaped hollow core PCF-SPR sensor and investigated the effect of air holes on the SPR sensing performance. The wavelength sensitivity of 2900 nm/RIU was achieved for RI (1.33,1.34) detection. J.N. Dash and R. Jha described a D-shape PCF-SPR sensor in which a silver-graphene layer as the sensitive materials was coated outside the fiber structure [15]. The amplitude sensitivity was 216 RIU−1 with the spectral sensitivity of 3700 nm/RIU for RI detection range in 1.33-1.37. G. An et al. [16] developed a D-shape PCF-SPR sensor with a rectangular lattice, and the plane of the polished fiber coated the nanoscale gold film. The maximum spectral sensitivity of the sensor in the RI range between 1.33 and 1.35 is about 2000 nm/RIU. One of the advantages of the D-shaped PCF-SPR sensors is that the sensitive metal layer can be coated adjacent to the core, which promotes strong interaction with the analyte, and results in enhanced sensing performance. The interaction between the plasmonic mode and fundamental mode depends on the structural parameters of the sensors. The coupling enhancement effect is not effective for some single D-shape PCF-SPR sensors due to the complicated structure [17]. However, it is an effective approach to enhance the coupling effects between the plasmonic mode and fundamental core guided mode by using two parallel D-shape PCFs. Most of the mode operations for reported D-shaped PCF-SPR sensors have been carried out in the visible wavelength range and RI range larger than 1.33, but relatively little efforts have been devoted to use two parallel fibers for lower RI detection (1.27–1.33). For many halogenated ethers and pharmaceuticals, their refractive indexes are located in the lower RI range [18], [19]. Therefore, the sensors with lower RI detection range offer great potential in the fields of pharmaceutical inspection and pharmaceutical leakage monitoring [20].

In this work, a novel SPR sensor based on parallel double D-shaped PCFs with a high sensitivity at near-infrared wavelengths is proposed and numerically analyzed. By using finite-element method (FEM), the characteristics of the sensor are numerically studied. The performance of a conventional D-shape PCF-SPR sensor is compared to that of the D-shape PCFs-SPR parallel-detection sensor. The results show that the maximum spectral sensitivity of 13500 nm/RIU is attained for the RI range from 1.27 to 1.32 and the resolution is 7.41 × 10−6 RIU.

2. Materials and Methods

The original structure of the sensor is shown in Fig. 1(a). The sensor is composed of four layers of air holes arranged in a hexagonal lattice and the gold layer is coated on the surface of the PCF plane. Gold and silver are extensively used as plasmonic materials. Although silver possesses a sharper resonance peak than gold, it is unstable and easily oxidized. Therefore, gold is chosen as the surface plasmon layer due to its chemical stability in this work. Compared to the micro-structured PCF coated with metal inside of the air holes, this sensor avoids the inhomogeneity of the gold layer. This D-shape PCF-SPR sensor contacts the analyte via the gold layer rather than requiring the analyte to fill the small air holes. The thickness of the gold layer is t_{Au} = 50 nm and the length of the gold layer is 6.5 μm. The dielectric constant of gold is expressed as [21]:

\[ \varepsilon_{Ag}(\omega) = \varepsilon_{\infty} - \frac{\omega_p^2}{\omega(\omega + i\omega_s)}, \]

where \( \varepsilon_{\infty} = 9.75, \omega_p = 1.36 \times 10^{16}, \omega_s = 1.45 \times 10^{14} \) is the dielectric constant, the plasma frequency, and the scattering frequency of gold, respectively.

It is well-known that the structure parameters have great influences on the performances of the sensors. Based on numerous simulations, the dimension parameters of the proposed two D-shaped PCFs-SPR sensor are determined as follows. The diameter of each D-shaped PCF is 9 μm, and the diameter of the perfectly matched layer (PML) is 11 μm. The pitch size of the cladding air hole is \( \Lambda = 1 \mu m \), the diameters of the air hole is \( d_o/\Lambda = 0.6 \), and the distance between the two D-shape
fibers is $d_x/\Lambda = 0.8$. RI of the analyte ($n_a$) is 1.27–1.32 and $n_a = 1.0$ is air RI. In the theoretical analysis, the D-shape fibers are considered to be made of silica glass and the RI of silica glass is calculated by the Sellmeier equation [22]:

$$n^2 - 1 = \frac{0.696166\lambda^2}{\lambda^2 - (0.0684043)^2} + \frac{0.4079426\lambda^2}{\lambda^2 - (0.1162414)^2} + \frac{0.897479\lambda^2}{\lambda^2 - (9.896161)^2}. \quad (2)$$

With regards to fabrication, the required D-shaped PCFs have been achieved by widely known etching or side polishing technique and have been reported in many literatures such as Ref. [13], thus the fabrication technology for D-shaped PCFs is available. Then the high pressure chemical vapor deposition (CVD) technique could be used to deposit metal layers on the plane of the D-shaped PCFs and offers good control of the outer metal layer thicknesses, allowing for uniformity along the whole fiber length [23]. It can be accomplished by accurately adjusting the distance between the two D-shaped PCFs with microscopy and fixed with the precision instruments. Although it is slightly difficult to manipulate the two D-shaped PCFs adjacent each other at nanoscale, yet it is reasonable to believe that this difficulty can be overcome under the assistance of modern nano-manufacturing technology.

For the D-shape fiber based on SPR sensing, the propagation loss $\alpha_{\text{loss}}$ is defined as [24]:

$$\alpha_{\text{loss}} = \frac{40\pi}{\lambda \ln 10} \text{Im}(n_{\text{eff}}) \times 10^6 \text{ (dB/m)} \approx 8.686 \text{Im}(n_{\text{eff}}) \frac{2\pi}{\lambda}. \quad (3)$$

The propagation loss of the sensor are numerically investigated by the FEM [24]. Fig. 1(b) shows the cross-sectional FEM mesh of the sensor. The calculating area is made of 14516 meshes, and a perfectly matched layer (PML) has 7293 elements. The vertex number is 466 and the minimum unit is $5.351 \times 10^{-6}$ in the structure.
3. Results

Fig. 2(a)–(f) display the electric field distributions of the core-guided mode for the even mode and odd mode at specific wavelengths. The scale bar in this figure represents the magnitude of the electric field. The red area is the largest distribution of light energy and the blue is the smallest distribution of light energy. Fig. 2(a)–(e) show most of the light energy distributes in the two cores and the metal surface. The light energy distributions of the core-guided mode are limited to the fiber core as shown in Fig. 2(f). The arrows represent the direction of the electric field. It can be obviously observed from Fig. 2 that light energy is transferred between the two cores, leading to improved strong-interaction coupling at the metal surface. There are no y-polarized modes as the geometrical fibre structure is not symmetrical in the x and y dimensions and the light energies between two fibers periodically change only in the direction of the x polarization. For the uncoated gold layer parallel D-shape PCFs, the total interference transverse electric field $\vec{E}(x, y, z)e^{-jwt}$ can be given as [25]:

$$\vec{E}(x, y, z)e^{-jwt} = M(x, y, z)e^{i\phi(x,y,z)}e^{j[(\beta_e+\beta_o)/2z - w]}$$

where $M = \sqrt{c_o^2 E_o^2 + c_e^2 E_e^2 + 2c_e c_o E_e E_o \cos[(\beta_e - \beta_o)z]}$ is the amplitude, $\phi = \tan^{-1}\left[\frac{c_o E_o - c_e E_e}{c_o E_o + c_e E_e} \times \tan(\frac{\beta_e - \beta_o}{2} z)\right]$ is the phase shift, $\beta_e$ and $\beta_o$ are the propagating constants of the fiber core-guided even and odd modes, respectively, and $c_o^2 + c_e^2 = 1$.

The power of the two cores $P_A$ and $P_B$ is given by:

$$\begin{cases} P_A(z) = M^2(-x, y, z) c_o^2 E_o^2(-x, y) + c_e^2 E_e^2(-x, y) + 2c_e c_o E_e E_o(\cos(\beta_e - \beta_o)z) \\ P_B(z) = M^2(x, y, z) c_o^2 E_o^2(x, y) + c_e^2 E_e^2(x, y) - 2c_e c_o E_e E_o(\cos(\beta_e - \beta_o)z) \end{cases}$$
Given that $E_{e}(-x, y) = E_{e}(x, y)$ and $E_{o}(-x, y) = -E_{o}(x, y)$, the transmission characteristics of the parallel D-shape PCF-SPR sensor can be derived for the parallel D-shape PCF coated with a gold layer.

The transmittance function $T'(z)$ is expressed as the ratio of the power transmitted from one core to another core and written as:

$$
T'(z) = \frac{P'_A(z)}{P'_B(0)} = \left[\frac{\psi(z)}{z}\right]^2 + \varphi(z) \times \sin^2\left(\frac{\beta_{e} - \beta_{o}}{2} z\right),
$$

where

$$
\psi(z) = 10^{-\left(\alpha_{ez}/20\right)} - 10^{-\left(\alpha_{oz}/20\right)}, \varphi(z) = 10^{-\left[(\alpha_{ez} + \alpha_{oz})z/20\right]}.
$$

For clarity and simplicity, we assume $c_{e} = c_{o}$ and $E_{e} = E_{o}$. $z$ is the propagation length of the optical fiber. When $z$ equals to zero, the optical power is mainly concentrated in the core B. Therefore, we can indicate that the incident energy is emitted in the core B and then transferred to the core A. The light energy is exchanged periodically between the two modes and so the amplitude of the two modes also changes periodically. During the periodic exchange of light energy between two fibers, more light energy coupled to the metal surface results in higher sensing sensitivity [25], [26].

Fig. 3 shows that the core-guided mode loss spectra for the odd mode and even mode of $x$-polarization. The black line and red line represent the loss spectra of the core-guided odd mode and even mode, respectively. There are three peaks in the spectra. The corresponding electric field distributions of the three resonant peaks as shown in Fig. 2(a)–(e). The peak with the largest propagation loss is denoted as the main peak and the others are designated as the secondary peaks. The peak in the loss spectrum of the core-guided mode indicates the resonant wavelength because the maximum energy is shifted from the core-guided mode to plasmonic mode at this wavelength. Several resonance peaks emerge due to coupling of the core-guided mode with higher order plasmonic modes [27]. In this study, the main peak is studied and more suitable for sensing detection because its resonant peak is the strongest. Fig. 2(c) and (d) show that the transferred energy of the odd mode at 1220 nm is more than that of the even mode. Fig. 3 further reveals a sharp loss peak at 1220 nm for the dispersion relations of the odd mode. The resonance intensity and depth of the odd mode are larger than those of the even mode. The resonance coupling of the odd mode at 1220 nm is stronger than that of the even mode. Therefore, the odd mode for $x$-polarization is selected to evaluate the performance of the proposed sensor in the subsequent analysis. Moreover, the resonance peak around 1220 nm is chosen for discussion because of its narrower bandwidth and higher resolution.

Fig. 4 displays the propagation loss spectra of the core-guided odd mode with the analyte RI range between 1.27 and 1.32. This refractive index range is located in the range of $1.27 < n < 1.35$ for biosensing detection [28]. The resonance wavelength shows the right move and the resonance...
depth increases with increasing analyte RI. It can be explanation that the absorption of gold layer relies on the environmental medium RI, the variation in absorption wavelength can be measured even if the change of sample RI is slight. Sensitivity is one of the important performance indicators of the sensor and needs to be evaluated in the analyte RI range. The spectral sensitivity $S$ is shown as [29]:

$$ S(\lambda) = \frac{\Delta \lambda_{\text{peak}}}{\Delta n_a} \text{ (nm/RIU)}, \quad (7) $$

The maximum variation in resonance wavelength is $\Delta \lambda_{\text{peak}} = 135$ nm and the maximum spectral sensitivity of 13500 nm/RIU is obtained when the change of the analyte RI is $\Delta n_a = 0.01$. The wavelength resolution of the detector is assumed to be $\Delta \lambda_{\text{min}} = 0.1$ nm and the RI resolution is represented as [30]:

$$ R = \frac{\Delta n_a \Delta \lambda_{\text{min}}}{\Delta \lambda_{\text{peak}}}. \quad (8) $$

Hence, assuming that the wavelength resolution of the detector for $\Delta \lambda_{\text{min}} = 0.1$ nm, the RI resolution of the sensor is estimated to be about $7.41 \times 10^{-6}$RIU.

Consider a signal to noise ratio (SNR) of 60 dB, the minimum full-width-at-half-maxima (FWHM) is 72.5 nm for $n_a = 1.32$, a sensitivity of 13500 nm/RIU in 1.27–1.32 is obtained using a rigorous definition for the detection limit of the SPR sensor proposed in Ref. [8] ($\sigma_n = \text{FWHM}/(4.5 \times S \times SNR^{0.25})$), a high sensing resolution of $4.29 \times 10^{-4}$ RIU is achievable.

For comparison, the cross-section and FEM mesh of the single D-shape PCF-SPR sensor are shown in Fig. 5. The structure of the single D-shape PCF-SPR sensor is the same as that of the parallel two D-shape PCFs. Figure 6 presents influence of the propagation loss with analyte RI between 1.29 and 1.32 for the single D-shape PCF-SPR sensor polarized along the $x$-axis. The resonance wavelength shows red shift and the resonance intensity increases when analyte RI from 1.29 to 1.32. Most of the energy is shifted from the fiber core to metal surface as shown in Fig. 6 [inset(b)]. In Fig. 6 [inset(a)] shows that the electric field distributions of the core-guided mode for the analyte RI $n_a = 1.30$, and almost all of the energy is concentrated in the fiber core outside the resonant wavelength. The maximum variation in resonance wavelength is $\Delta \lambda_{\text{peak}} = 30$ nm and the maximum spectral sensitivity of 3000 nm/RIU is achieved. For the single D-shape sensor, the light energy is only in the single $x$-direction shifted from the core-guided mode to plasmonic mode. In comparison, for the parallel two D-shape sensor, the light energy is transferred from core A to core B and the amplitude of the two modes changes periodically. Therefore, more power is transferred to the plasmonic mode resulting in greater efficiency and intensity of resonance coupling. It can be seen that the sensing property of the parallel two D-shape PCFs is superior to that of the single
Fig. 5. (a) Cross-section structure and (b) FEM mesh of the single D-shape PCF-SPR sensor.

Fig. 6. Propagation loss curves of x-polarization mode for analyte RI between 1.29 and 1.32 of the single PCF with insets (a) and (b) showing the field distributions at different wavelengths.

D-shape PCF. Table 1 lists the key parameters for the sensing performance of PCF-SPR sensors with different structures. It is seen from Table 1 that the performance of the proposed parallel two PCFs-SPR sensor is not only better than that of the single D-shape PCF-SPR sensor, but also higher than that of other sensors.

The effects of geometrical parameters on the parallel two PCFs-SPR sensor are investigated while the other parameters are kept the same. Fig. 7 describes the propagation loss of the odd mode for different thicknesses of the gold layer (tAu) between 30 nm and 60 nm. A slight blueshift occurs and the resonance peaks reduces gradually when the thickness of the gold layer is increased. Consequently, it is possible to tune and optimize the sensor performance such as the operation range and amount of loss precisely by adjusting the thickness of the gold layer [31]. It is seen from Fig. 7 that the propagation loss decreases with increasing the thickness of gold layer. The resonance peak of the 50 nm layer is sharper than that of the 30 nm layer, indicating the sensor possesses a higher sensitivity for the 50 nm gold layer. Therefore, the thickness of gold layer is determined to be 50 nm in the following discussion.
Table 1  
Key Parameters Associated With the Sensing Performance of Various PCF-SPR Sensors

<table>
<thead>
<tr>
<th>Fiber structure</th>
<th>Detection RI range (RIU)</th>
<th>Operation Wavelength range (nm)</th>
<th>Average Sensitivity (nm/RIU)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Multi-core flat, PCF-SPR</td>
<td>1.46-1.485</td>
<td>1240-1420</td>
<td>9600</td>
<td>[3]</td>
</tr>
<tr>
<td>Simple D-shape, PCF-SPR</td>
<td>1.33-1.43</td>
<td>550-1770</td>
<td>9800</td>
<td>[12]</td>
</tr>
<tr>
<td>MOF, PCF-SPR</td>
<td>1.33-1.34</td>
<td>550-750</td>
<td>2900</td>
<td>[14]</td>
</tr>
<tr>
<td>Silver-Graphene D-shape, PCF-SPR</td>
<td>1.33-1.37</td>
<td>480-660</td>
<td>3700</td>
<td>[15]</td>
</tr>
<tr>
<td>Parallel two D-shape, PCF-SPR</td>
<td>1.27-1.32</td>
<td>720-1680</td>
<td>13500</td>
<td>This work</td>
</tr>
</tbody>
</table>

The distance between the parallel two fibers is one of important factors determining the sensitivity and resolution. Fig. 8 shows the propagation loss curves of different distances between two D-shape fibers. A slight red-shift occurs when \( \frac{d_c}{\Lambda} \) ranges from 0.4 to 1.2. The resonance intensity increases when \( \frac{d_c}{\Lambda} \) changes from 0.4 nm to 0.8 nm, while the resonance intensity decreases with \( \frac{d_c}{\Lambda} \) increasing from 0.8 to 1.2. This can be explained by the following reasons. Firstly, when the distance is smaller, the parallel two D-shape fibers are similar to a single dual-core fiber and the...
resonance intensity is weaker because the coupling interaction is dominated by the coupling of the core-guided mode and plasmonic mode in single dual-core structure. Secondly, when the distance increases, the periodic couplings between two fibers increase gradually besides the coupling effect of the core-guided mode and plasmonic mode, leading to the intensity increasing of total couplings. Lastly, the interaction effects of the periodic couplings between two fibers decrease with the further increasing of the distance, which is similar to the case of two independent single fibers. Hence, 0.8 is chosen as the distance in our analysis.

Fig. 9 shows the propagation loss curves of the odd mode for the parallel D-shape sensors when \( d_a/\Lambda = 0.8 \), \( t_{Au} = 50 \text{ nm} \), and \( n_2 = 1.30 \).

4. Conclusion

A parallel dual D-shape PCF-SPR sensor for near-infrared wavelengths is described and resonance coupling is studied systematically. Light energy is shifted from core A to core B and exchanged periodically between the two modes. The sensing performance of the proposed sensor is improved because the amplitude of the two modes changes periodically and more core energy is transferred to the surface plasmonic energy. For the RI range from 1.27 to 1.32, the maximum spectral sensitivity
of 13500 nm/RIU and the resolution of $7.41 \times 10^{-6}$ RIU are achieved. The proposed PCFs-SPR sensor has promising applications in drug inspection and monitoring.

References